

Algebra 2

	Key Standards Covered	Possible Resources
<p>Quarter 1 September 6- November 2</p>	<ul style="list-style-type: none"> ● Perform arithmetic operation with complex numbers: HSN-CN.A.1, 2, ● Use complex numbers in polynomial identities and equations: HSN-CN.C.7, 8 ● Interpret functions that arise in applications in terms of the context: HSF-IF.B.4, 5, 6 ● Build new functions from existing functions: HSF-IF.B.1, 3 ● Interpret the structure of expressions: HSA-SSE.A.1a, 1b, 2, ● Write expressions in equivalent forms to solve problems: HSA-SSE.B.3a ● Understand the relationship between zeros and factors of polynomials: HSA-APR.B.3 ● Create equations that describe numbers or relationships: HSA-CED.A.1, 2, 3 ● Represent and solve equations and inequalities graphically: HSA-REI.D.11 	<ul style="list-style-type: none"> ● Homework given after each class ● Practice questions showing understanding of concept (both individually and in groups). <ul style="list-style-type: none"> ○ Using ideas like think-pair-share ● Quizzes administered after each lesson is completed to show knowledge gained. ● Scavenger hunt review to show if students are prepared for unit test. ● Test administered at the end of the unit to show knowledge gained within the unit.
	Key Standards Covered	Possible Resources

<p>Quarter 2 November 12- January 28</p>	<ul style="list-style-type: none"> ● Using complex numbers in polynomial identities and equations: HSN-CN.C.7, 8, 9 ● Interpret the structure of expressions: HSA-SSE.A.1a, 1b, 2 ● Understand the relationship between zeros and factors of polynomials: HSA-APR.B.2, 3 ● Use polynomial identities to solve problems: HSA-APR.C.4, 5, 6 ● Represent and solve equations and inequalities graphically: HSA-REI.D.11 ● Interpret functions that arise in applications in terms of the context: HSF-IF.B.4, 5, 6, C.7, 8 ● Build new functions from existing functions: HSF-BF.B.3 	<ul style="list-style-type: none"> ● Homework given after each class ● Practice questions showing understanding of concept (both individually and in groups). <ul style="list-style-type: none"> ○ Using ideas like think-pair-share ● Quizzes administered after each lesson is completed to show knowledge gained. ● Activity for test review (independent or small group) ● Test administered at the end of the unit to show knowledge gained within the unit.
	Key Standards Covered	Possible Resources
<p>Quarter 3 February 4- April 5</p>	<ul style="list-style-type: none"> ● Interpret the structure of expressions: HSA-SSE.A.2 ● Create equations that describe the number of relationships: HSA-CED.A.4 ● Understand solving equations as a process of reasoning and explain the reasoning: HSA-REI.A.2 ● Analyze functions using different representations: HSF-IF.C.7b, 8 ● Build a function that models a relationship between two quantities: HSF-BF.A.1b ● Build new functions from existing functions: HSF-BF.B.4a 	<ul style="list-style-type: none"> ● Homework given after each class ● Practice questions showing understanding of concept (both individually and in groups). <ul style="list-style-type: none"> ○ Using ideas like think-pair-share ● Quizzes administered after each lesson is completed to show knowledge gained. ● Activity for test review (independent or small group) ● Test administered at the end of the unit to show knowledge gained within the unit.
	Key Standards Covered	Possible Resources

Quarter 4 April 8- June 17	<ul style="list-style-type: none"> ● Interpret the structure of expressions: HSA-SSE.A.1a, 1b ● Write expressions in equivalent forms to solve problems: HSA-SSE.B.3c ● Create equations that describe numbers: HSA-CED.A.1, 2, 3 ● Represent and solve equations and inequalities graphically: HSA-REI.D.11 ● Analyze functions using different representation: HSF-IF.C.7e, 8, 9 ● Build a function that models a relationship between quantities: HSF-BF.A.1b ● Build new functions for existing functions: HSF-BF.B.4a ● Construct and compare linear and exponential models and solve problems: HSF-LE.4 ● Extend the domain of trigonometric functions using the unit circle: HSF-TF.A.1, 2 ● Model periodic phenomena with trigonometric functions: HSF-TF.B.6 ● Define trigonometric ratios and solve problems involving right triangles: HSG-SRT.C.6 ● Apply trigonometry to general triangles: HSG-SRT.D.11 	<ul style="list-style-type: none"> ● Homework given after each class ● Practice questions showing understanding of concept (both individually and in groups). <ul style="list-style-type: none"> ○ Using ideas like think-pair-share ● Quizzes administered after each lesson is completed to show knowledge gained. ● Activity for test review (independent or small group) ● Test administered at the end of the unit to show knowledge gained within the unit.
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AUL Curriculum - Mathematics - Algebra II

Title of Unit	Quadratic Equations and Functions	Grade Level	10, 11, 12
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Curriculum Area	Algebra II	Time Frame	5-7 Weeks
Developed By	Douglas Frost		
Identify Desired Results (Stage 1)			
Content Standards			
<ul style="list-style-type: none"> • Perform arithmetic operation with complex numbers: HSN-CN.A.1, 2, • Use complex numbers in polynomial identities and equations: HSN-CN.C.7, 8 • Interpret functions that arise in applications in terms of the context: HSF-IF.B.4, 5, 6 • Build new functions from existing functions: HSF-IF.B.1, 3 • Interpret the structure of expressions: HSA-SSE.A.1a, 1b, 2, • Write expressions in equivalent forms to solve problems: HSA-SSE.B.3a • Understand the relationship between zeros and factors of polynomials: HSA-APR.B.3 • Create equations that describe numbers or relationships: HSA-CED.A.1, 2, 3 • Represent and solve equations and inequalities graphically: HSA-REI.D.11 			
Understandings		Essential Questions	
Overarching Understanding		Overarching	Topical
<ul style="list-style-type: none"> • Identify the vertex, line of symmetry, maximum or minimum, domain, range, and translations of a quadratic function. • Graph quadratic functions with and without graphing calculators. • Use quadratic functions as models. • Graph transformations of the parent quadratic function $y = x^2$. • Compare translations to the parent quadratic function. • Identify the x-intercepts of the graph of related quadratic functions. • Solve quadratic equations. 		<ul style="list-style-type: none"> • What are the advantages of a quadratic function in vertex form? in standard form? • How is any quadratic function related to the parent quadratic function $y = x^2$? • How are real solutions of a quadratic equation related to the graph of the 	<ul style="list-style-type: none"> • What is the vertex and axis of symmetry of the quadratic function? • What factors of the constant term will add up to the coefficient of the middle term? • How many and what type of solutions are there in the
Related Misconceptions			

<ul style="list-style-type: none"> • Stating the opposite location of the vertex based on the given function. • Plugging in the wrong numbers when finding the vertex algebraically and using the Quadratic Formula. • Finding factors of the coefficients of the middle term that add up to the constant term. 		<p>given equation?</p> <ul style="list-style-type: none"> • What factor of the given number is a perfect square?
<p>Knowledge Students will know...</p>	<p>Skills Students will be able to...</p>	
<ul style="list-style-type: none"> • The vertex is the turning point of a parabola and can determine where the axis of symmetry is located. • The discriminant of the Quadratic Formula can determine the types of solutions that exist with a given equation. • The imaginary number i is defined as $\sqrt{-1}$. 	<ul style="list-style-type: none"> • Graph quadratic functions with and without a calculator. • Determine the transformation of any quadratic function based on the parent quadratic function $y = x^2$. • Find the vertex, axis of symmetry, and x-intercepts of the graph of a quadratic function both graphically and algebraically. • Solve quadratic equations. 	
<p>Assessment Evidence (Stage 2)</p>		
<p>Performance Task Description</p>		

- Graph quadratic functions. (HSF-IF.B.1, 3, 4, 5, 6)
 - Visual representation of quadratic functions.
 - Use the graph to find key information in a real-world situation
 - Examples include the vertex to find the highest point an object will hit and how long will it take for the same object to hit the ground.
- Determine the transformation of the graph of a quadratic function based on the parent quadratic function $y = x^2$. (HSF-IF.B.1, 3, 4, 5, 6)
 - Using the different forms of quadratic functions (standard, vertex, and intercept), determine the different transformations that occur based on the parent quadratic function.
- With the general form of a quadratic equation $ax^2 + bx + c = 0$, use Completing the Square to derive the Quadratic Formula. (HSA-REI.B.4b)
 - Algebraically, solve the general form of a quadratic equation for x using Completing the Square.

Other Evidence

- Homework given after each class
- Practice questions showing understanding of concept (both individually and in groups).
 - Using ideas like think-pair-share
- Quizzes administered after each lesson is completed to show knowledge gained.
- Scavenger hunt review to show if students are prepared for unit test.
- Test administered at the end of the unit to show knowledge gained within the unit.

Learning Plan (Stage 3)

General Information

- All warm-up questions, provided by the publisher, will lead into the new section of the unit by having students think outside-the-box.
 - Example: When starting to solve quadratic equations, determine the graph of a quadratic function that will produce a smile on a given face given the parabola will have two, one, and no x -intercepts.
- This unit is part of both Algebra I and Algebra II. However, in Algebra II, we introduce quadratic systems and imaginary numbers.
- Throughout the unit, students will have access to online assessments and practice problems provided by the publisher for self-assessment.
- The activities below can be delivered in individual or small groups.

Sequence

- Graphing quadratic functions based on the given form (standard, vertex, intercept) with and without a graphing calculator.
 - Identify the vertex, axis of symmetry, and intercepts, if possible
 - In small groups, determine the transformation(s) performed on a given graph based on the parent quadratic function.
 - Find the vertex and axis of symmetry without graphing based on the form of the function given
- Modeling quadratic functions.
 - Illustrating how quadratic functions are utilized in the real world.
 - Using the knowledge gained from graphing quadratic functions, students will create their own quadratic functions and real-world examples for their classmates to solve.
- Factor quadratic expressions.
 - Review of finding factors of composite numbers.
 - Choosing the correct factors to properly factor a quadratic expression
- Solve quadratic equations by factoring, Completing the Square, and the Quadratic Formula.
 - Utilize factoring to solve equations.
 - Introduce Completing the Square to solve any type of quadratic equation.
 - In small groups, use Completing the Square to derive the Quadratic Formula.
- Introduce complex numbers.
 - Review simplifying radical expressions.
 - Illustrate how the square root of a negative number can now be simplified using i .
- Unit assessment on Quadratic Equations and Functions.
 - Utilize the problems created by students either as review or test questions.

Title of Unit	Polynomial and Polynomial Functions	Grade Level	10, 11, 12
Curriculum Area	Algebra II	Time Frame	5-7 Weeks
Developed By	Douglas Frost		
Identify Desired Results (Stage 1)			
Content Standards			
<ul style="list-style-type: none"> Using complex numbers in polynomial identities and equations: HSN-CN.C.7, 8, 9 Interpret the structure of expressions: HSA-SSE.A.1a, 1b, 2 Understand the relationship between zeros and factors of polynomials: HSA-APR.B.2, 3 Use polynomial identities to solve problems: HSA-APR.C.4, 5, 6 Represent and solve equations and inequalities graphically: HSA-REI.D.11 Interpret functions that arise in applications in terms of the context: HSF-IF.B.4, 5, 6, C.7, 8 Build new functions from existing functions: HSF-BF.B.3 			
Understandings		Essential Questions	
Overarching Understanding		Overarching	Topical
<ul style="list-style-type: none"> Write a polynomial function given a polynomial equation. Identify the degree of a polynomial equation. Identify the highest power of a polynomial function. Write a polynomial given its factors or zeros. Identify the zeros of a polynomial function by finding the x-intercepts of its graph. Factor a polynomial equation. Apply the Zero-Product Property 		<ul style="list-style-type: none"> What does the degree of a polynomial tell you about its related polynomial function? For a polynomial function, how are factors, zeros, and x-intercepts related? For a polynomial 	<ul style="list-style-type: none"> What factor(s) of the constant term are solutions to the given polynomial equation? What degree is the given polynomial? How many x-intercepts are there in the
Related Misconceptions			

<ul style="list-style-type: none"> • Finding numbers that add up to the constant instead of multiply to. • The number of turning points is equal to the degree of the polynomial. • Remembering the rules of factoring quadratic expressions. 	<p>equation, how are factors and roots related?</p>	<p>given polynomial?</p>
<p>Knowledge Students will know...</p>	<p>Skills Students will be able to...</p>	
<ul style="list-style-type: none"> • Polynomials functions are polynomials of degree 3 or higher. • Degree of a given polynomial is also the number of solutions in the polynomial equation. • When graphing polynomials, the number of turning points possible is one less than the degree of the polynomial function. • When solving polynomial equations, you will need to utilize synthetic division to simplify the polynomial to a quadratic expression. 	<ul style="list-style-type: none"> • Graph polynomial functions. • Solve polynomial equations when you are given a factor of the polynomial. • Divide polynomials using long and synthetic division. • Utilize synthetic division to solve polynomial equations. 	
<p>Assessment Evidence (Stage 2)</p>		
<p>Performance Task Description</p>		
<ul style="list-style-type: none"> • Creating a diorama (HSF-IF.B.4, 5, 6, C.7, 8, 9; HSF-BF.B.3) <ul style="list-style-type: none"> ○ Based on a given sheet of cardboard, determine the dimensions of a diorama that needs to be a certain volume. • Graphing polynomial functions (HSA-APR. B.3) <ul style="list-style-type: none"> ○ Given the factored form of a polynomial function, graph the function. <ul style="list-style-type: none"> ■ Use the zeros to determine the location of the turning points. 		
<p>Other Evidence</p>		

- Homework given after each class
- Practice questions showing understanding of concept (both individually and in groups).
 - Using ideas like think-pair-share
- Quizzes administered after each lesson is completed to show knowledge gained.
- Activity for test review (independent or small group)
- Test administered at the end of the unit to show knowledge gained within the unit.

Learning Plan (Stage 3)

General Information

- All warm-up questions, provided by the publisher, will lead into the new section of the unit by having students think outside-the-box.
 - Example: Determine the fraction based on given properties (Numerator is a factor of 6, Denominator is a factor of 4, etc.).
- Throughout the unit, students will have access to online assessments and practice problems provided by the publisher for self-assessment.
- The activities below can be delivered in individual or small groups.

Sequence

- Polynomial functions
 - Introduce the classification of polynomials and key terms.
 - In small groups and student-centered, determine the properties of polynomials when graphed.
 - Based on this, the students will determine the generalizations of end behavior and turning points.
 - Determine the end behavior of a polynomial without graphing.
- Polynomial factors and zeros
 - Graph polynomials with a calculator
 - Using the calculator, identify the relative minimum and maximum of the function.
 - Determine the zeros of a polynomial graphically
 - Given either the zeros or factors of a polynomial, write the polynomial function
- Solving polynomial equations, part 1
 - In small groups, solve simple polynomial equations
 - Utilizes the principles of solving quadratic equations
 - Some equations need to be simplified to quadratic form
- Dividing polynomials
 - Illustrate the similarities to numerical and polynomial division
 - Utilize small groups to divide polynomials using synthetic division
- Solving polynomial equations, part II
 - Deals with utilizing the Rational Root Theorem and Fundamental Theorem of Algebra
 - Determine which rational root will simplify the polynomial
 - In small groups, find all the zeros of a polynomial function

Title of Unit	Function Operations and Square Root Functions	Grade Level	10, 11, 12
Curriculum Area	Algebra II	Time Frame	4-6 Weeks
Developed By	Douglas Frost		
Identify Desired Results (Stage 1)			
Content Standards			
<ul style="list-style-type: none"> ● Interpret the structure of expressions: HSA-SSE.A.2 ● Create equations that describe the number of relationships: HSA-CED.A.4 ● Understand solving equations as a process of reasoning and explain the reasoning: HSA-REI.A.2 ● Analyze functions using different representations: HSF-IF.C.7b, 8 ● Build a function that models a relationship between two quantities: HSF-BF.A.1b ● Build new functions from existing functions: HSF-BF.B.4a 			
Understandings		Essential Questions	
Overarching Understanding		Overarching	Topical
<ul style="list-style-type: none"> ● Simplify radical expressions. ● Solve radical equations. ● Determine the domain of radical functions. ● Check for extraneous solutions. ● Find inverse functions. ● Graph functions and their inverses. 		<ul style="list-style-type: none"> ● To simplify the nth root of an expression, what must be true about the expression? ● When you square each side of an equation, is the 	<ul style="list-style-type: none"> ● What factor of the given number or expression is a perfect square? ● What is the domain of the given function?
Related Misconceptions			

<ul style="list-style-type: none"> • An expression where the exponent is not 2 and even (Ex: y^4) is not a perfect square. • After squaring both sides of an equation, there are two answers. • When doing the composition of two functions, you plug the first function in the list into the second function. 	<p>resulting equation equivalent to the original?</p> <ul style="list-style-type: none"> • How are a function and its inverse related? 	<ul style="list-style-type: none"> • Does the given function have an inverse?
<p>Knowledge Students will know...</p>	<p>Skills Students will be able to...</p>	
<ul style="list-style-type: none"> • How similar solving radical equations are to other types of equations taught so far. • The different operations that can be performed on functions. • The graph of the inverse of a function is a reflection of the original graph over the line $y = x$. 	<ul style="list-style-type: none"> • Simplify radical expressions. • Solve radical equations. • Perform function operations. • Find the inverse of a function. • Graph radical functions. 	
<p>Assessment Evidence (Stage 2)</p>		
<p>Performance Task Description</p>		
<ul style="list-style-type: none"> • Analyzing the Dimensions of a Yacht (HSA-CED.A.4, HSA-REI.A.2, HSF-IF.C.7b, 8) <ul style="list-style-type: none"> ○ Using the given inequality, determine by the dimensions given of a boat would be allowed to sail in the America's Cup. ○ If not, determine what dimensions to change in order for the boat to be allowed to sail. • Properties of Exponents (HSN-RN.A.1) <ul style="list-style-type: none"> ○ Reviewing the properties of exponents taught in Algebra I • Graphing Inverses (HSF-BF.B.4a) <ul style="list-style-type: none"> ○ Using a graphing calculator, graph the inverse of a given function. ○ Utilize the graph to determine if a function has a true inverse. 		
<p>Other Evidence</p>		

- Homework given after each class
- Practice questions showing understanding of concept (both individually and in groups).
 - Using ideas like think-pair-share
- Quizzes administered after each lesson is completed to show knowledge gained.
- Activity for test review (independent or small group)
- Test administered at the end of the unit to show knowledge gained within the unit.

Learning Plan (Stage 3)

General Information

- All warm-up questions, provided by the publisher, will lead into the new section of the unit by having students think outside-the-box.
 - Example: Given the distance from a cell phone tower and its range, determine how many miles do you have to finish your call.
- Throughout the unit, students will have access to online assessments and practice problems provided by the publisher for self-assessment.
- The activities below can be delivered in individual or small groups.

Sequence

- Roots and Radical Expressions
 - Simplifying radical expressions
- Multiplying and Dividing Radical Expressions
 - In small groups, multiply and divide given radical expressions
- Graphing Radical Functions
 - Graph radical functions
 - Determine the domain and range of a radical function without graphing.
- Solving Square Roots and Other Radical Equations
 - Solving radical equations
 - Students will work on their own to solve radical equations based on solving by solving linear and quadratic equations (by taking the square root) to show its similarity.
- Function Operations
 - In small groups, students will perform the four basic operations on functions.
 - Find the composition of two functions.
- Inverse Relations and Functions
 - Determine if a function has an inverse.
 - Find the inverse of a function.
 - Graph the inverse of a function,

Title of Unit	Exponential and Logarithmic Functions	Grade Level	10, 11, 12
Curriculum Area	Algebra II	Time Frame	5-7 Weeks
Developed By	Douglas Frost		
Identify Desired Results (Stage 1)			
Content Standards			
<ul style="list-style-type: none"> ● Interpret the structure of expressions: HSA-SSE.A.1a, 1b ● Write expressions in equivalent forms to solve problems: HSA-SSE.B.3c ● Create equations that describe numbers: HSA-CED.A.1, 2, 3 ● Represent and solve equations and inequalities graphically: HSA-REI.D.11 ● Analyze functions using different representation: HSF-IF.C.7e, 8, 9 ● Build a function that models a relationship between quantities: HSF-BF.A.1b ● Build new functions for existing functions: HSF-BF.B.4a ● Construct and compare linear and exponential models and solve problems: HSF-LE.4 			
Understandings		Essential Questions	
Overarching Understanding		Overarching	Topical
<ul style="list-style-type: none"> ● Model situations with exponential functions. ● Use exponents to solve logarithmic equations and logarithms to solve exponential equations. ● Show that exponents and logarithms are inverse functions. ● Graph exponential and logarithmic functions. 		<ul style="list-style-type: none"> ● How do you model a quantity that changes regularly over time by the same percentage? ● How are exponents and 	<ul style="list-style-type: none"> ● What logarithmic base is used when solving exponential equations? ● Based on the given
Related Misconceptions			

<ul style="list-style-type: none"> • Exponent is now a variable instead of a number. • Graph of exponential functions looks like a parabola. • Growth rate of exponential functions is constant. • When writing logarithms, the numbers are in the wrong position. • Not utilizing natural logarithms when the base of the given exponential function is e. 	<p>logarithms related?</p> <ul style="list-style-type: none"> • How are exponential functions and logarithmic functions related? 	<p>exponential model, are you experiencing exponential growth or decay?</p> <ul style="list-style-type: none"> • What property or properties of logarithms would you need to utilize to expand or condense the given expression?
<p>Knowledge Students will know...</p>	<p>Skills Students will be able to...</p>	
<ul style="list-style-type: none"> • Exponential functions have a faster growth or decay rate than linear functions. • Logarithms are used to find the exponent you need to raise the base to achieve the given number. • The properties of logarithms are used to either condense or expand a given expression. • The natural number e was derived by Leonhard Euler and it is based on a pattern. 	<ul style="list-style-type: none"> • Graph and evaluate exponential and logarithmic functions. • Utilize the properties of logarithms to expand or condense a given expression. • Solve exponential and logarithmic equations. 	
<p>Assessment Evidence (Stage 2)</p>		
<p>Performance Task Description</p>		

- .Apparent Magnitudes of Stars (HSF-IF.7e, 8, 9, HSA-REI.D.11)
 - Determine the magnitude of different stars in the night sky.
- Graphing Exponential and Logarithmic Functions (HSF-IF.7e, HSA-SSE.A.1b, HSA-CED.A.2, HSF-IF.C.8)
 - Graph exponential and logarithmic functions.
 - Differentiate the differences between exponential and linear functions.
- Fitting Curve to Data (HSF-IF.B.4)
 - Based on the given data, determine the type of regression model is best used (linear, logarithmic, exponential)

Other Evidence

- Homework given after each class
- Practice questions showing understanding of concept (both individually and in groups).
 - Using ideas like think-pair-share
- Quizzes administered after each lesson is completed to show knowledge gained.
- Activity for test review (independent or small group)
- Test administered at the end of the unit to show knowledge gained within the unit.

Learning Plan (Stage 3)

General Information

- All warm-up questions, provided by the publisher, will lead into the new section of the unit by having students think outside-the-box.
 - Example: You won the grand prize on a gameshow. Do you take \$10,000 a week for a year or 1¢ today, 2¢ tomorrow, 4¢ the next day, and continue the pattern for a year?
- Throughout the unit, students will have access to online assessments and practice problems provided by the publisher for self-assessment.
- The activities below can be delivered in individual or small groups.

Sequence

- Exponential Models and Functions.
 - Illustrate the differences between linear and exponential functions.
 - Graph exponential functions.
 - In small groups, create an exponential model based on a given real-world situation and compute.
- Logarithmic Functions
 - Graph logarithmic functions.
 - Using graphing, illustrate how exponential and logarithmic functions are inverses of each other.
 - In small groups, determine the rules of transformations of the graphs logarithmic functions.
 - Evaluate logarithmic expressions
- Properties of Logarithms
 - Introduce the properties of logarithms by using the inverse relationship between exponential and logarithmic functions.
 - Expand and condense logarithmic expressions
- Solving Exponential and Logarithmic Equations
 - Without assistance, solve exponential and logarithmic equations based on the similarities of solving linear, radical, and simple exponential equations (when the base is the exponent).
 - Write and solve exponential and logarithmic equations based on a given real-world situation.
 - Some models will need the students to create the model (Ex: Exponential growth and decay, compound interest)

Title of Unit	Trigonometric Ratios and Functions	Grade Level	10, 11, 12
Curriculum Area	Algebra II	Time Frame	6-8 Weeks
Developed By	Douglas Frost		
Identify Desired Results (Stage 1)			
Content Standards			
<ul style="list-style-type: none"> Extend the domain of trigonometric functions using the unit circle: HSF-TF.A.1, 2 Model periodic phenomena with trigonometric functions: HSF-TF.B.6 Define trigonometric ratios and solve problems involving right triangles: HSG-SRT.C.6 Apply trigonometry to general triangles: HSG-SRT.D.11 			
Understandings		Essential Questions	
Overarching Understanding		Overarching	Topical
<ul style="list-style-type: none"> Use trigonometric functions, Find the value of the reciprocal trigonometric functions based on the corresponding trigonometric functions. Introduce radian measure and show how the circumference of the unit circle relates to it. Utilize inverse trigonometric functions to find the measure of an angle formed by two sides. Apply the Law of Sines and Law of Cosines to find missing parts of non-right triangles. 		<ul style="list-style-type: none"> If you know the value of $\sin \theta$, how can you find $\cos \theta$, $\tan \theta$, $\csc \theta$, $\sec \theta$, and $\cot \theta$? What is the purpose of the inverse trigonometric function? How can you find missing 	<ul style="list-style-type: none"> What is the value of a given trigonometric function for a given angle? What is the measure of the angle formed by these two sides? What angle has the value for a specific
Related Misconceptions			

<ul style="list-style-type: none"> Using the improper trigonometric function to find the missing part of a triangle. Secant and Sine functions are reciprocals of each other. Same with cosine and cosecant. The period is the number of number of times the curve is repeated within 2π radians. Computing the exact value of a trigonometric function at angles that are multiples of 30° or 45°. 	<p>information on a triangle that does not contain a right angle?</p>	<p>specific trigonometric function?</p>
<p>Knowledge Students will know...</p>	<p>Skills Students will be able to...</p>	
<ul style="list-style-type: none"> There are six trigonometric functions, where the new three functions are reciprocals of the original three trigonometric functions. The unit circle is utilized to find the value of any trigonometric function and is the basis to the the graphs of the sine and cosine functions. Radian measure deals with length in terms of π. The inverse trigonometric functions are used to find the measure of an angle. When to use the Law of Sines and Law of Cosines. 	<ul style="list-style-type: none"> Find the value of any trigonometric function based on the unit circle. Convert degree measure to radians and vice versa. Find the measure of an angle given two sides of a triangle. Use the Law of Sines and Law of Cosines to find the missing part of a non-right triangle. 	
<p>Assessment Evidence (Stage 2)</p>		
<p>Performance Task Description</p>		

- Measuring Radians (HSF-TF.A.1)
 - Develop a tactile understanding of radian measure.
- Determining the Length of a Zipline (HSF-TF.C.9, HSG-SRT.C.6, 8, D.9, 10, 11)
 - Use trigonometric identities to find certain lengths within the diagram.
 - Use the laws and the Half Angle Identity to find the angle of depression of the zipline.
- The Ambiguous Case (HSG-SRT.D.11)
 - Even though two triangles have one pair of congruent angles and two pairs of congruent sides, the angle you are looking for using the Law of Sines may be incorrect.
 - Students will need to remember the sine function is also positive in Quadrant II.

Other Evidence

- Homework given after each class
- Practice questions showing understanding of concept (both individually and in groups).
 - Using ideas like think-pair-share
- Quizzes administered after each lesson is completed to show knowledge gained.
- Activity for test review (independent or small group)
- Test administered at the end of the unit to show knowledge gained within the unit.

Learning Plan (Stage 3)

General Information

- All warm-up questions, provided by the publisher, will lead into the new section of the unit by having students think outside-the-box.
 - Example: A ferris wheel takes 20 minutes to go around once. How far off the ground are you after 5 and 10 minutes? At what time(s) will you be 474 feet above the platform?
- Throughout the unit, students will have access to online assessments and practice problems provided by the publisher for self-assessment.
- The activities below can be delivered in individual or small groups.

Sequence

- Trigonometric Functions with Right Triangles
 - Review sine, cosine, and tangent functions
 - Introduce cosecant, secant, and cotangent functions.
 - In small groups, evaluate the trigonometric values for special angles/
 - Utilize the 30-60-90 and 45-45-90 triangles.
 - Solve right triangles
- Angles and the Unit Circle and Radian Measure
 - Illustrate how the unit circle is used to determine the measure of an angle in a circle on the coordinate plane.
 - In small groups, determine the sine and cosine of an angle when given a point on the terminal side of the angle.
 - Without any assistance, in small groups, students will do the Measuring Radian assessment.
 - Convert degree measure to radians and vice versa.
 - Find the coordinate of the general angles of the unit circle utilizing the special triangles.
- Evaluating Trigonometric Functions of Any Angle
 - Utilizing the given point on the terminal side and the Pythagorean Theorem, find the value of each trigonometric function.
 - Utilize a reference angle when the terminal side is located in Quadrants II, III, or IV.
- Inverse Trigonometric Functions
 - Introduce trigonometric inverse functions
 - Students need to remember there are two solutions unless the inverse they are doing is -1, 0, or 1.
 - Students will create trigonometric word problems based on everything taught up to this point.
- Area and Law of Sines
 - Find the area of a non-right triangle using trigonometry.
 - Formula will be derived from the warm-up exercise.
 - Use the area formula to derive the Law of Sines,
 - Utilize the Law of Sines to find missing side/angle.
- Law of Cosines
 - On their own, based on the warm-up, derive the Law of Cosines
 - Warm-up illustrates how the cosine of an angle can be computed if the lengths of all three sides are given.
 - In small groups, work on questions where the students must decide to use either the Law of Sines or the Law of Cosines.

